

# A Methodological Construction of an Efficient Sequential Consistency Protocol\*

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## Abstract

*A concurrent object is an object that can be concurrently accessed by several processes. Sequential consistency is a consistency criterion for such objects. Informally, it states that a multiprocess program executes correctly if its results could have been produced by executing that program on a single processor system. (Sequential consistency is weaker than atomic consistency -the usual consistency criterion- as it does not refer to real-time.) The paper proposes a simple protocol that ensures sequential consistency when the shared memory abstraction is supported by the local memories of nodes that can communicate only by exchanging messages through reliable channels. Differently from other sequential consistency protocols, the proposed protocol does not rely on a strong synchronization mechanism such as an atomic broadcast primitive or a central node managing a copy of every shared object. From a methodological point of view, the protocol is built incrementally starting from the very definition of sequential consistency. It has the noteworthy property of providing fast writes operations (i.e., a process has never to wait when it writes a new value in a shared object). According to the current local state, some read operations can also be fast. An experimental evaluation of the protocol is also presented. The proposed protocol could be used to manage Web page caching.*

## 1 Introduction

**Sequential consistency** The definition of a consistency criterion is crucial for the correctness of a multiprocess program. Basically, a consistency criterion defines which value has to be returned when a read operation on a shared object is invoked by a process. The strongest (i.e., most constraining) consistency criterion is *atomic consistency* [15] (also called *linearizability* [10]). It states that a read returns the value written by the last preceding write, “last”

referring to real-time occurrence order (concurrent writes being ordered). *Causal consistency* [3, 5] is a weaker criterion stating that a read does not get an overwritten value. Causal consistency allows concurrent writes; consequently, it is possible that concurrent read operations on the same object get different values (this occurs when those values have been produced by concurrent writes). Other consistency criteria (weaker than causal consistency) have been proposed [1, 21].

This paper focuses on *sequential consistency* [12]. This criterion lies between atomic consistency and causal consistency. Informally it states that a multiprocess program executes correctly if its results could have been produced by executing that program on a single processor system. This means that an execution is correct if we can totally order its operations in such a way that (1) the order of operations in each process is preserved, and (2) each read obtains the last previously written value, “last” referring here to the total order. The difference between atomic consistency and sequential consistency lies in the meaning of the word “last”. This word refers to real-time when we consider atomic consistency, while it refers to a logical time notion when we consider sequential consistency (namely the logical time defined by the total order). The main difference between sequential consistency and causal consistency lies in the fact that (as atomic consistency) sequential consistency orders all write operations, while causal consistency does not require to order concurrent writes.

Atomic consistency is relatively easy to implement in a distributed message-passing system. Each process  $p_i$  maintains in a local cache the current value  $v$  of each shared variable  $x$ , and such a cached value  $v$  is systematically invalidated (or updated) each time a process  $p_j$  writes  $x$ . The conflicts due to multiple accesses to a shared variable  $x$  are usually handled by associating a manager  $M_x$  with every shared variable  $x$ . One of the most known atomic consistency protocols is the invalidation-based protocol due to Li and Hudak [13] that has been designed to provide a dis-

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tributed shared memory on top of a local area network. An update-based atomic consistency protocol is described in [8].

Due to its very definition, atomic consistency requires that the value of a variable  $x$  cached at  $p_i$  be invalidated (or updated) each time a process  $p_j$  issues a write on  $x$ . In that sense, the atomic consistency criterion (that is an abstract property of a computation) is intimately related to an *eager* invalidation (or update) mechanism (that concerns the operational side). Said in another way, atomic consistency is a consistency criterion that can be too *conservative* for some applications.

Differently, sequential consistency can be seen as a form of *lazy* atomic consistency [19]. A cached value has not to be systematically invalidated each time the corresponding shared variable is updated. Old and new values of a shared variable can coexist at different processes as long as the resulting execution could have been produced by running the multiprocess program on a single processor system. Of course, a protocol implementing sequential consistency can be more involved than a protocol implementing atomic consistency, as it has to keep track of global information allowing it to know, for each process  $p_i$ , which old values currently used by  $p_i$  have to be invalidated (or updated) and which ones have not. This global information tracking, which is at the core of sequential consistency protocols, is the additional price that has to be paid to replace eager invalidation by lazy invalidation, thereby providing the possibility for efficient runs of multiprocess programs.

**Related work: Sequential consistency protocols.** Several protocols providing a sequentially consistent shared memory abstraction on top of an asynchronous message passing distributed system have been proposed. The protocol described in [2] implements a sequentially consistent shared memory abstraction on top of a physically shared memory and local caches. It uses an atomic  $n$ -queue update primitive. Attiya and Welch [7] present two sequential consistency protocols. Both protocols assume that each local memory contains a copy of the whole shared memory abstraction. They order the write operations using an atomic broadcast facility: all the writes are sent to all processes and are delivered in the same order by each process. Read operations issued by a process are appropriately scheduled to ensure their correctness.

The protocol described in [17] considers a server site that has a copy of the whole shared memory abstraction. The local memory of each process contains a copy of a shared memory abstraction, but the state of some of its objects can be invalid. When a process wants to read an object, it reads its local copy if it is valid. When a process wants to read an object whose state is invalid, or wants to write an object, it sends a request to the server. In that way the server orders all write operations. An invalidation mechanism ensures

that the reading by  $p_i$  of an object that is locally valid is correct. A variant of this protocol is described in [4]. The protocol described in [18] uses a token that orders all write operations and piggybacks updated values like one of the protocols described [7] it provides fast (i.e., purely local) read operations [9]<sup>1</sup>.

Most of the previous protocols rely on a strong synchronization mechanism that has a scope spanning the whole system (atomic broadcast facility, navigating token, or central manager<sup>2</sup>). Differently, the protocol described in [19] is fully distributed in the sense that it does not rely on an underlying global mechanism: each object  $x$  is managed by its own object manager  $M_x$  and there is no synchronization primitive whose scope is the entire system.

**Content of the paper.** This paper presents a methodological construction of a sequential consistency protocol. A variant of this protocol has first been presented in [11], where a dynamically adaptive and parameterized algorithm that implements sequential consistency, cache consistency or causal consistency, according to the setting of some parameter. This parameterized algorithm is presented “from scratch”, without exhibiting or relying on basic underlying principles. Here, we show that a variant of its sequential consistency instantiation can be obtained from a simple derivation starting from the very definition of sequential consistency.

The algorithm we obtain from the derivation not only is surprisingly simple, but -as it is based on the very essence of sequential consistency- it reveals to be particularly efficient for some classes of applications. The protocol has the nice property to allow the write operations to be fast, i.e., a write operation is always executed locally without involving global synchronization. Differently, some read operations can be fast, while other cannot. The fact that a read operation is fast or not depends on the variable that is read and the set of variables that have been previously written by the process issuing the read operation, so it is context-dependent.

The paper is made up of five sections. Section 2 presents the computation model, and defines sequential consistency. Then, Section 3 derives the protocol from the sequential consistency definition. Section 4 presents experimental results that show the protocol performance. Finally, Section 5 concludes the paper.

## 2 The Sequentially Consistent Shared Memory Abstraction

A parallel program defines a set of processes interacting through a set of concurrent objects. This set of shared

<sup>1</sup>As shown in [7] atomic consistency does not allow protocols in which all read operations (or all write operations) are fast [10, 16]. Differently, causal consistency allows protocols where all operations are fast [3, 5, 20].

<sup>2</sup>E.g., an atomic broadcast facility allows ordering all the write operations, whatever the processes that issue them.

objects defines a *shared memory abstraction*. Each object is defined by a sequential specification and provides processes with operations to manipulate it. When it is running, the parallel program produces a concurrent system [10]. As in such a system an object can be accessed concurrently by several processes, it is necessary to define consistency criteria for concurrent objects.

A shared memory system is composed of a finite set of sequential processes  $p_1, \dots, p_n$  that interact via a finite set  $X$  of shared objects. Each object  $x \in X$  can be accessed by read and write operations. A write into an object defines a new value for the object; a read allows to obtain a value of the object. A write of value  $v$  into object  $x$  by process  $p_i$  is denoted  $w_i(x)v$ ; similarly a read of  $x$  by process  $p_j$  is denoted  $r_j(x)v$  where  $v$  is the value returned by the read operation;  $op$  will denote either  $r$  (read) or  $w$  (write). To simplify the analyses, as in [3, 15, 20], we assume all values written into an object  $x$  are distinct<sup>3</sup>. Moreover, the parameters of an operation are omitted when they are not important. Each object has an initial value (it is assumed that this value has been assigned by an initial fictitious write operation).

**History concept** Histories are introduced to model the execution of shared memory parallel programs. The *local history* (or local computation)  $\hat{h}_i$  of  $p_i$  is the sequence of operations issued by  $p_i$ . If  $op1$  and  $op2$  are issued by  $p_i$  and  $op1$  is issued first, then we say “ $op1$  precedes  $op2$  in  $p_i$ ’s process-order”, which is noted  $op1 \rightarrow_i op2$ . Let  $h_i$  denote the set of operations executed by  $p_i$ ; the local history  $\hat{h}_i$  is the total order  $(h_i, \rightarrow_i)$ .

**Definition 1** An execution history (or simply history, or computation)  $\hat{H}$  of a shared memory system is a partial order  $\hat{H} = (H, \rightarrow_H)$  such that:

- $H = \bigcup_i h_i$
- $op1 \rightarrow_H op2$  if:
  - i)  $\exists p_i : op1 \rightarrow_i op2$  (in that case,  $\rightarrow_H$  is called process-order relation),
  - or ii)  $op1 = w_i(x)v$  and  $op2 = r_j(x)v$  (in that case  $\rightarrow_H$  is called read-from relation),
  - or iii)  $\exists op3 : op1 \rightarrow_H op3$  and  $op3 \rightarrow_H op2$ .

Two operations  $op1$  and  $op2$  are *concurrent* in  $\hat{H}$  if we have neither  $op1 \rightarrow_H op2$  nor  $op2 \rightarrow_H op1$ .

**Legality notion** The legality concept is the key notion on which are based definitions of shared memory consistency criteria [3, 5, 16, 21]. From an operational point of view, it states that, in a legal history, no read operation can get an overwritten value.

<sup>3</sup>Intuitively, this hypothesis can be seen as an implicit tagging of each value by a pair composed of the identity of the process that issued the write plus a sequence number.

**Definition 2** A read operation  $r(x)v$  is legal if: (i)  $\exists w(x)v : w(x)v \rightarrow_H r(x)v$  and (ii)  $\nexists op(x)u : (u \neq v) \wedge (w(x)v \rightarrow_H op(x)u \rightarrow_H r(x)v)$ . A history  $\hat{H}$  is legal if all its read operations are legal.

Sequential consistency has been proposed by Lamport in 1979 to define a correctness criterion for multiprocessor shared memory systems [12]. A system is sequentially consistent with respect to a multiprocess program, if “the result of any execution is the same as if (1) the operations of all the processors were executed in some sequential order, and (2) the operations of each individual processor appear in this sequence in the order specified by its program.”

This informal definition states that the execution of a program is sequentially consistent if it could have been produced by executing this program on a single processor system<sup>4</sup>. More formally, we define sequential consistency in the following way. Let us first recall the definition of *linear extension* of a partial order. A linear extension  $\hat{S} = (S, \rightarrow_S)$  of a partial order  $\hat{H} = (H, \rightarrow_H)$  is a topological sort of this partial order. This means we have the following: (i)  $S = H$ , (ii)  $op1 \rightarrow_H op2 \Rightarrow op1 \rightarrow_S op2$  ( $\hat{S}$  maintains the order of all ordered pairs of  $\hat{H}$ ) and (iii)  $\rightarrow_S$  defines a total order.

**Definition 3** A history  $\hat{H} = (H, \rightarrow_H)$  is sequentially consistent if it has a legal linear extension.

## 3 Methodological Construction of a Sequential Consistency Protocol

### 3.1 Underlying Distributed System

Our aim is to implement the sequentially consistent shared memory abstraction on top of an underlying message-passing distributed system. Such a system is a distributed system made up of  $n$  reliable sites, one per process (hence, without ambiguity,  $p_i$  denotes both a process and the associated site). Each  $p_i$  has a local memory. The processes communicate through reliable channels by sending and receiving messages. There are no assumptions neither on process speed, nor on message transfer delay. Hence, the underlying distributed system is reliable but asynchronous.

### 3.2 The Methodology

The usual approach to design sequential consistency protocols consists in first defining a protocol and then proving it is correct. The approach we adopt here is different, in the sense that we start from the very definition of sequential consistency and *derive* from it a sequential consistency protocol. More precisely, to ensure that a distributed execution

<sup>4</sup>In his definition, Lamport assumes that the *process-order* relation defined by the program (point 2 of the definition) is maintained in the equivalent sequential execution, but not necessarily in the execution itself. As we do not consider programs but only executions, we implicitly assume that the *process-order* relation displayed by the execution histories are the ones specified by the programs which gave rise to these execution histories.

$\widehat{H} = (H, \rightarrow_H)$  has an equivalent legal sequential history  $\widehat{S} = (H, \rightarrow_S)$ , we (1) first, define a base legal sequential history  $\widehat{S}$ , and (2) then, design a protocol that controls the execution of the multiprocess program in order to produce an actual distributed execution  $\widehat{H}$  equivalent to the base history  $\widehat{S}$ .

The first subsection that follows derives a trivial sequential consistency protocol that works for a very particular type of multiprocess programs; these particular multiprocess programs have the nice property that all operations can be executed locally. Then, by observing that the history of each sequential process can be decomposed in segments such as those considered in the previous type of multiprocess programs, a new sequential consistency protocol is derived that works for the general case. Finally, the last subsection shows how to enhance such a general protocol in order to achieve higher efficiency.

### 3.3 Step 1 of the Construction: Considering a Trivial Case

Let us start with a multiprocess program where the sequential history  $\widehat{h}_i$  of each process  $p_i$  has the following very particular structure; namely,  $\widehat{h}_i$  is  $R_i^0$  followed by  $WR_i^1$  where  $R_i^0$  is a (possibly empty) sequence containing only read operations, and  $WR_i^1$  is a (possibly empty) sequence starting with a write operation and followed by write operations on any variable and read operations only on variables that have been previously written by  $p_i$  (i.e., if  $r_i(x)$  appears in  $WR_i^1$  then  $w_i(x)$  appears previously in  $WR_i^1$ ).

Figure 1 shows an example of program as described in the above paragraph (in order to facilitate the presentation and without loss of generality, the figures that illustrate the construction consider a multiprocess program made up of  $n = 3$  processes).

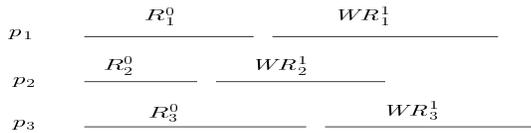


Figure 1. A (very) simple case

As we can see from the very definition of sequential consistency, the parallel execution described in Figure 1 could have been produced by executing sequentially, first  $R_1^0$ ,  $R_2^0$ , and  $R_3^0$  in any order (they contain only read operations that obtain the initial values of the shared variables), and then  $WR_1^1$ ,  $WR_2^1$ , and  $WR_3^1$  in any order (as any read operation appearing in  $WR_i^1$  reads only variables that  $p_i$  has previously written)<sup>5</sup>.

It follows that, if all the multiprocess programs had the structure previously described ( $\widehat{h}_i$  being  $R_i^0$  followed by

<sup>5</sup>Let us observe that sequential consistency does not require that all the caches containing a copy of a shared variable  $x$  have to be equal at the end of the computation.

$WR_i^1$ ), an implementation would simply consist in providing each process  $p_i$  with a local cache containing all the shared variables. No additional protocol would be necessary. So, we assume in the following that each process  $p_i$  has a local cache denoted  $C_i[x]$  associated with each shared variable  $x$ .

### 3.4 Step 2 of the Construction: (General Case) Looking for Correctness

Let us first observe that, in the general case, the history  $\widehat{h}_i$  of a sequential process  $p_i$  can always be decomposed into consecutive “segments” (subsequences), each segment being of the form  $R_i^k$  or  $WR_i^k$ , namely (“,” stands for “followed by”):

$$\widehat{h}_i = R_i^0, WR_i^1, R_i^1, WR_i^2, R_i^2, \dots, WR_i^k, R_i^k, \dots$$

where, as before,  $R_i^k$  is a (possibly empty) sequence of only read operations,  $WR_i^k$  is a (possibly empty) sequence starting with a write operation and followed by write operations on any shared variable or read operations on shared variables previously written in  $WR_i^k$ . It is important to notice that, for  $k > 0$ ,  $R_i^k$  starts (and consequently  $WR_i^k$  ends) when  $p_i$  reads a shared variable not written in  $WR_i^k$ .

Controlling a distributed execution will consist in two types of actions. The first concerns the safety of read operations, namely it consists in blocking the read of a shared variable  $x$  issued by a process  $p_i$  when the current value of  $C_i[x]$  would produce a non-legal read. The second concerns liveness, namely it consists in propagating the new values to ensure that no read can block forever.

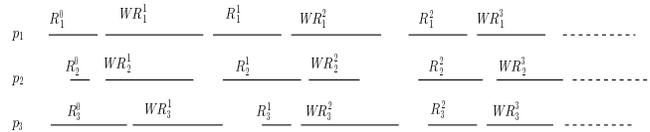
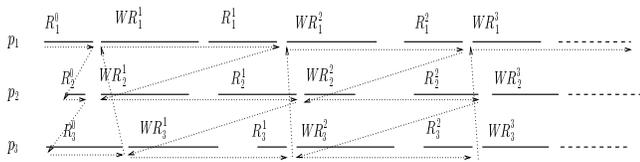


Figure 2. An execution

The decomposition of each process history into segments and the particular case of a single segment examined in Section 3.3, provides us with some hint on how to define a base legal sequential history  $\widehat{S}$ . Let us consider the execution described in Figure 2. A base legal sequential history  $\widehat{S}$  that benefits from the segment decomposition of process histories can be the following:

$$\widehat{S} = R_1^0, R_2^0, R_3^0, \boxed{WR_1^1, R_1^1}, \boxed{WR_2^1, R_2^1}, \boxed{WR_3^1, R_3^1}, \boxed{WR_1^2, R_1^2}, \boxed{WR_2^2, R_2^2}, \boxed{WR_3^2, R_3^2}, \dots$$

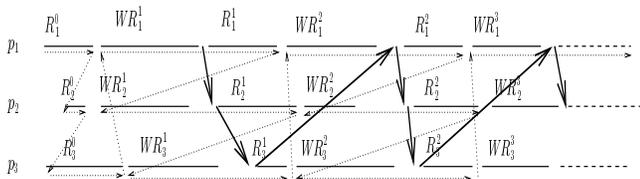
This base sequential execution can be produced by a mono-processor system whose scheduler provides the control first to  $p_1$  to execute  $R_1^0$ , to  $p_2$  to execute  $R_2^0$ , and to



**Figure 3. A base sequential execution  $\widehat{S}$**

$p_3$  to execute  $R_3^0$ , and then to  $p_1$  to execute  $WR_1^1, R_1^1$ , then to  $p_1$  to execute  $WR_2^1, R_2^1$ , etc. (This execution is indicated with the dotted arrows in Figure 3.)

As indicated, designing a sequential consistency protocol consists of ensuring that the actual distributed execution  $\widehat{H}$  is equivalent to the base sequential execution  $\widehat{S}$ . Let us observe that, in  $\widehat{S}$ , when  $p_2$  executes  $R_2^1$ , it can read the value of a variable  $x$  that has been written by  $p_1$  when it executed  $WR_1^1$ . Hence,  $p_2$  must be informed of these writes before it executes  $R_2^1$ . A simple way to attain this goal consists of using a token (traveling along a logical ring so that no process misses updates, e.g.,  $p_1, p_2, \dots, p_n, p_1$ ) and carrying the last value it knows of each shared variable. To carry the new values written in  $WR_1^1$ , the token has to be sent after  $WR_1^1$ . Moreover, as  $R_1^1$  modifies no shared variables, it can be sent by  $p_1$  before  $R_1^1$ . So, when a process  $p_i$  has the token, it ends a segment  $WR_i^k$ , sends the token and starts a segment  $R_i^k$ .



**Figure 4. Using a token to disseminate the updates and prevent deadlock**

The travel of the token is indicated by the bold arrows in Figure 4. Let us observe that for  $\widehat{H}$  (the distributed execution) to be equivalent to  $\widehat{S}$ , the values carried by the token when it arrives at a process (say  $p_2$  in Figure 4) have to be considered only if they have not been overwritten by  $WR_2^1$ . This means that we have to manage the token exactly as if it was received by  $p_2$  just after  $p_2$  has executed  $R_2^0$  and was sent by  $p_2$  to  $p_3$  just after  $p_2$  has terminated  $R_2^1$ : logically, the token follows the dotted arrows so that  $\widehat{H}$  is equivalent to  $\widehat{S}$ .

The resulting protocol is described in Figure 5. As already indicated,  $X$  denotes the set of shared variables, and  $C_i[x]$  is  $p_i$ 's local cache containing the value of the shared variable  $x$ . Each process  $p_i$  maintains a boolean array  $updated_i$  such that  $updated_i[x]$  is true iff  $p_i$  has updated  $x$  since the last visit of the token. The boolean  $no\_change_i$

is a synonym for  $\bigwedge_{y \in X} (\neg updated_i[y])$  ( $no\_change_i$  is true iff no shared variable has been updated since the last visit of the token at  $p_i$ ). The write operation and the statements associated with the token reception are executed atomically. (Let us observe that the arrival of the token at a process always corresponds to the beginning of a new segment for that process.)<sup>6</sup>

**init:**

**for each**  $y \in X$  **do**

$C_i[y] \leftarrow$  initial value of  $y$ ;  $updated_i[y] \leftarrow false$ ;

**end do;**

$no\_change_i \leftarrow true$ ;

The token (with initial values) is initially at  $p_1$  that simulates its arrival at the end of  $WR_1^1$ ;

**operation**  $w_i(x)v$ : %  $w_i(x)v$  always belongs to some segment  $WR_i^z$  %

$C_i[x] \leftarrow v$ ;

$updated_i[x] \leftarrow true$ ;  $no\_change_i \leftarrow false$ ;

**return()**

**operation**  $r_i(x)$ :

**wait until** ( $no\_change_i \vee updated_i[x]$ );

%  $no\_change_i \Rightarrow r_i(x) \in R_i^z \wedge updated_i[x] \Rightarrow r_i(x) \in WR_i^z$  %

**return** ( $C_i[x]$ )

**upon reception of token**[ $X$ ]:

**for each**  $y \in X$  **such that**  $\neg updated_i[y]$  **do**

$C_i[y] \leftarrow token[y]$ ;

**end do;**

**for each**  $y \in X$  **such that**  $updated_i[y]$ ; **do**

$token[y] \leftarrow C_i[y]$ ;  $updated_i[y] \leftarrow false$ ;

**end do;**

**send token**[ $X$ ] to the next process on the logical ring;

$no\_change_i \leftarrow true$ ;

% we have here:  $\forall y \in X : updated_i[y] = false$  %

**Figure 5. Protocol for process  $p_i$ : token-based version**

### 3.5 Step 3 of the Construction: (General Case) Looking for Efficiency

When we look carefully at the way the token is used in the previous protocol, we observe that it plays actually two distinct roles. On one side, when it is at a process  $p_i$ , the token gives  $p_i$  the right to disseminate the updates of the shared variables. That is the “control part” associated with the token: it provides an exclusive right to its current owner (a single process at a time can disseminate updates), and establishes an order among the processes to exploit this exclusive right. On another side, when it is sent by  $p_i$  to  $p_j$ , the token carries updates. That is the “communication” part

<sup>6</sup>The reader familiar with token-based termination detection protocols [14] can see that the protocol described in Figure 5 and these termination detection protocols share the same underlying mechanism combining token and flags (here, the flags  $no\_change_i$ ). The corresponding flags in a termination detection protocol are usually called  $contpassive_i$ , and are used to know if a process  $p_i$  stayed continuously passive between two consecutive visits of the token. This flag is set to *false* when  $p_i$  receives a message. It is reset to *true* when  $p_i$  owns the token, becomes passive and sends the token to its successor.

```

init:
for each  $y \in X$  do
   $C_i[y] \leftarrow$  initial value of  $y$ ;  $updated_i[y] \leftarrow false$ ;
end do;
 $no\_change_i \leftarrow true$ ;
 $next_i \leftarrow 1$ ;

operation  $w_i(x)v$ : %  $w_i(x)v$  always belongs to some segment  $WR_i^z$  %
 $C_i[x] \leftarrow v$ ;
 $updated_i[x] \leftarrow true$ ;  $no\_change_i \leftarrow false$ ;
return()

operation  $r_i(x)$ :
wait until ( $no\_change_i \vee updated_i[x]$ );
%  $no\_change_i \Rightarrow r_i(x) \in R_i^z \wedge updated_i[x] \Rightarrow r_i(x) \in WR_i^z$  %
return ( $C_i[x]$ )

Task T:
(1) loop case ( $next_i = i$ ) then let  $upd = \{(y, C_i[y]) \mid updated_i[y]\}$ ;
(2)   for each  $j \neq i$  do send  $UPDATES(upd)$  to  $p_j$  end do;
(3)   for each  $(y, v_y) \in upd$  do  $updated_i[y] \leftarrow false$  end do;
(4)    $no\_change_i \leftarrow true$ ;
(5)   ( $next_i \neq i$ ) then wait ( $UPDATES(upd)$  from  $next_i$ );
(6)   for each  $(y, v_y) \in upd$  do
(7)     if ( $\neg updated_i[y]$ ) then  $C_i[y] \leftarrow v_y$  end if
(8)   end do;
(9)   end case;
(10)   $next_i \leftarrow (next_i \bmod n) + 1$ ;
(11) end loop

```

**Figure 6. Efficient protocol (for process  $p_i$ )**

associated with the token. This section shows that it is possible to dissociate these two distinct roles to get a more efficient protocol.

Let us first introduce a local variable  $next_i$ , such that  $next_i = i$  means that  $p_i$  (knows that it) has the token and is consequently allowed to disseminate updates. More generally,  $next_i = j$  means that, from  $p_i$ 's point of view,  $p_j$  is the process that is currently allowed to disseminate updates. So, circulating the token along the logical ring  $p_1, p_2, \dots, p_n, p_1, \dots$ , is realized by having each  $next_i$  variable taking successively the values  $1, 2, \dots, n, 1, \dots$

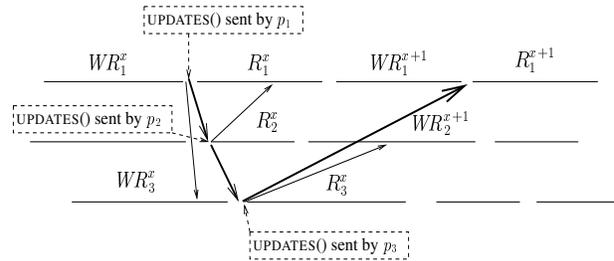
To dissociate the two roles of the token, the token itself is suppressed (as just indicated, it is replaced by the variables  $next_i$ ) and the statement associated with its management is replaced by a task denoted  $T$  (see Figure 6). (The write and read operations and the task  $T$  are executed atomically.) This task defines two distinct behaviors for a process  $p_i$  according to the token role. More precisely, when  $p_i$  has the token (case  $next_i = i$ ), it is allowed to send to the rest of processes all the updates it has done since the previous visit of the token (lines 1-2). These updates are carried by the message  $UPDATES(upd)$ . After it has sent its updates,  $p_i$  resets its local control variables (lines 3-4).

There are two main differences with respect to the previous token-based protocol. First, a process broadcasts only its own updates, and second, this broadcast is done eagerly.

(In the previous protocol, the token accumulates and disseminate the updates in a sequential way, following the logical ring.) This eager update dissemination, described in Figure 7, allows a process to be informed of new values earlier than what is done by the protocol of Figure 5 (in this figure, the  $UPDATES()$  messages "simulating" the token are described in bold arrows).

For a process  $p_i$ , the token passes from  $p_j$  to  $p_{j+1}$  when,  $next_i$  being equal to  $j$ ,  $p_i$  executes  $next_i \leftarrow (next_i \bmod n) + 1$  (line 10). All the processes have the same view of the order in which the token visits the processes. Consequently, after it has received and processed an  $UPDATES()$  message from  $p_{i-1}$ , the process  $p_i$  knows that it has the token: no explicit message is necessary to represent the token.

When  $p_i$  has not the token (case  $next_i \neq i$ ), it waits for an  $UPDATES()$  message from the next process allowed to broadcast its updates ( $p_{next_i}$ ). When it receives that message (line 5),  $p_i$  updates accordingly its local cache (as in the previous protocol, lines 6-7). This constitutes an early refreshing of its local cache with the new values provided by  $p_{next_i}$ .



**Figure 7. Eager dissemination of the updates**

It is important to notice that all the processes update their local caches (with the new values coming from the other processes) in the same order. This is an immediate consequence of the fact that each process  $p_i$  delivers the  $UPDATES()$  messages in the order defined by the successive values of  $next_i$ . As in the base token-based protocol,  $p_i$ 's own updates are done at the time  $p_i$  issues the corresponding write operations and tracked with the boolean array  $updated_i$ . These boolean flags are used to maintain the consistency of  $p_i$ 's local cache each time it receives and processes an  $UPDATES()$  message. More precisely, let us consider  $p_i$  that receives an  $UPDATES()$  message from  $p_j$ . There are two cases: (1)  $p_i$  is executing a  $WR_i^z$  segment when it receives an  $UPDATES()$  message from  $p_j$ . In that case,  $p_i$  updates its local cache, but as the updates overwritten by  $p_i$  are discarded (line 7), the resulting behavior is exactly the same as if all the updates included in the  $UPDATES()$  message had been applied to  $p_i$ 's local cache before  $WR_i^z$ . (2)  $p_i$  is executing a  $R_i^z$  segment when it receives an  $UPDATES()$  message from  $p_j$ . Let  $WR_j^y$  be the segment that terminated just before  $p_j$  sent the  $UPDATES()$  message. (Let us remind

that such a message is always sent after a  $WR_j^y$  segment and before the  $R_j^z$  segment that follows it.) Then,  $R_i^z$  can be divided in two sub-segments  $R1_i^z$  and  $R2_i^z$  separated by the processing of  $p_j$ 's UPDATES() message. The base sequential execution  $\hat{S}$  is now refined as follows:  $R1_i^z$  appears before  $WR_j^y$  (as  $p_i$  does not yet know the new values carried by the UPDATES() message), while  $R2_i^z$  appears after  $WR_j^y$  (as, after it has processed the UPDATES() message,  $p_i$  knows these values).

Finally, it is possible, from an engineering point of view, to adapt this protocol to particular environments. A simple adaptation would consist in allowing some processes  $p_i$  to keep the token for some time when they have it (i.e., when they are such that  $next_i = i$ ). The benefit of such a possibility depends on the read/write access pattern of the upper layer application program.

#### 4 Performance Evaluation

This section presents experiments that show the efficiency of the proposed protocol. Its performance is also compared with that of the popular sequential protocols proposed by Attiya and Welch [7]. The protocol described in Figure 6 is denoted CFJR in the following.

processes	FD	MM	FFT
2	99.53%	99.93%	99.35%
4	99.94%	99.99%	99.95%
8	99.86%	99.99%	99.97%

**Figure 8. Ratio of fast read operations per process**

**Context of the experiment** Note first that in our protocols all memory operations are fast except some read operations. (Recall that a memory operation is fast if it can be completed based only on the local state of the process that issued it.) An operation  $r_i(x)$  is blocking if, since the last visit of the token,  $p_i$  has not updated  $x$  (i.e.,  $updated_i[x]$  is false) while no other variable has been updated (i.e.,  $no\_change_i$  is true). Such a read operation blocks until the process receives the token in the first protocol, or until  $next_i = i$  in the second.

An analytic evaluation of how many read operations the protocol allows to be fast is not possible as it depends on the read/write patterns of the upper layer distributed application. Hence, we have used real benchmark implementations to estimate the number of fast reads and, more generally, to evaluate the protocol performance. Our experimental study has considered the protocol of Figure 6. We have implemented this protocol and three typical parallel processing applications: finite differences (FD), matrix multiplication (MM), and fast Fourier transform (FFT). We have implemented FD and MM (as in [22]), and FFT (as in [6]). The code, written in C, uses the *sockets* interface

	DD			MM		
	2	4	8	2	4	8
CFJR	2228.3	2360.0	1450.8	3760.0	3307.5	2813.3
AW- <i>fast<sub>r</sub></i>	14133.3	19100.0	22591.7	4816.7	10346.7	8718.3
AW- <i>fast<sub>w</sub></i>	12141.7	16400.0	21008.3	4348.3	9720.8	7512.5

	FFT		
	2	4	8
CFJR	554.2	512.5	437.5
AW- <i>fast<sub>r</sub></i>	1371.7	14070.0	11304.2
AW- <i>fast<sub>w</sub></i>	1227.5	10215.8	9093.3

**Figure 9. Execution time of DD, MM and FFT (in seconds)**

with UDP/IP for computer intercommunication<sup>7</sup>.

**Experimental results on the protocol efficiency** The results that follow concern the protocol described in Figure 6 (denoted CFJR, in short) running with the following application programs: (1) FD with  $16384 \times 1024$  elements, (2) MM with  $1600 \times 1600$  matrices, and (3) FFT with 262144 coefficients. The executions have been done in an experimental environment formed by a cluster of 2, 4 and 8 computers connected with a network. Each computer is a PC running Linux Red-Hat with a 1.5GHz AMD CPU, and 512Mbytes of RAM memory. The network is a switched, full-duplex 1Gbps Ethernet. We have mapped one process to each computer and have restricted our implementation to a maximum of 100 memory operations carried in one single message. Figure 8 shows the percentage of fast read operations in each process for the previously described FD, MM, and FFT application programs. As it can be observed, almost all read operations are fast in each case.

**Comparing the protocol with other protocols** We compare our protocol with two sequential consistency protocols proposed by Attiya and Welch [7]. The comparison is done with respect to two important performance measures: (1) the time used to run an application (i.e., its execution time), and (2) the number of messages sent through the network. Attiya and Welch have proposed a sequential consistency protocol where all read operations are fast while the write operations are not fast, which we denote by AW-*fast<sub>r</sub>*. They have also proposed a sequential consistency protocol with all write operations are fast while the read operations are not fast, which we denote by AW-*fast<sub>w</sub>*. We have executed these protocols with the same set of parallel applications (namely, FD, MM, and FFT), and in the same experimentation cluster.

Figure 9 presents the execution time (in seconds) of running FD, MM, and FFT using each sequential consistency protocol. It can be seen that, whatever the case, the execution

<sup>7</sup>The source code can be found at <http://luna.dat.esctet.urjc.es/~ernes>.

DD			
	2	4	8
CFJR	2667/50	960/29	579/11
AW-fast <sub>r</sub>	366361/190201	352321/264241	312321/308281
AW-fast <sub>w</sub>	346613/170453	342284/254204	338782/294742

MM			
	2	4	8
CFJR	3004/63	396/0.4	208/1.5
AW-fast <sub>r</sub>	110400/51520	110080/76800	109847/89367
AW-fast <sub>w</sub>	110080/51200	106587/73307	108239/87590

FFT			
	2	4	8
CFJR	5206/3357	376/87	194/15
AW-fast <sub>r</sub>	19922/4980	20970/8388	21068/9731
AW-fast <sub>w</sub>	19546/4604	19766/7184	19559/8426

**Figure 10. Total number (in thousands) of messages+acks sent by each process**

time provided by our protocol is much lower than with the other protocols.

Figure 10 presents the total number of messages and acknowledgments (in thousands) sent by each process when executing FD, MM, and FFT. By acknowledgments we mean all the messages sent to preserve the correct behavior of the protocol but without containing write operations. We can see that our protocol reduces in two orders of magnitude the total number of messages sent by each process. This is due to the fact that while our protocol pieces together several write operations in a single message (in our implementation, up to 100), each other protocol issues one message per write operation. Figure 10 also show that almost each message contains write operations in our protocol. Differently, more than 50% of the messages are acknowledgments in AW-fast<sub>r</sub> and AW-fast<sub>w</sub>.

## 5 Conclusion

This paper has presented a new sequential consistency protocol. Differently from the previous protocols we are aware of, this one has been derived from the very definition of the sequential consistency criterion. Due to its design principles, the protocol we have obtained is particularly simple. It provides fast write operations: these operations are always executed “locally” (i.e., without requiring any form of global synchronization). Read operations can also be fast when they are on a variable that has just been previously updated by the same process. An experimental study has been done. It shows that the proposed protocol is particularly efficient for a large class of multiprocess programs.

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